



## Algebraic Proof

Exam Style Questions

1. Jane says that the product of any two prime numbers is always odd. Jane is wrong. Explain why.

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(1 mark)

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2. Jackson thinks that  $n^2 + 5n + 1$  is always a prime number for all integer values of  $n$ . Is he correct?

Yes

No

Give a reason to support your answer.

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(2 marks)

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# JP Maths Revision

3.  $n$  is a positive integer. Aria says that expression  $n^2 + 3n + 2$  can never be prime. Explain why Aria is correct.

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(2 marks)

4. Susan says that the product of a square number and a cube number is always even. Give an example to prove that Susan is wrong.

$$\square \times \square = \square$$

(1 mark)

5.  $A$  is a positive even integer.  $B$  is a negative integer. Complete the following table.

	Sometimes true	Always true	Never true.
$AB$ is odd			
$A + B$ is positive.			
$A^3 B$ is negative.			

(2 marks)



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6. Match up the following descriptions to expressions:

Any two numbers
Two consecutive numbers
Two consecutive even numbers
Two consecutive odd numbers
Any two even numbers
Any two odd numbers
Two square numbers
Two multiples of 8

$n^2, m^2$
$2n + 1, 2n + 3$
$n, n + 1$
$n, m$
$2n, 2m$
$8n, 8m$
$2n, 2n + 2$
$2n + 1, 2m + 1$

(3 marks)

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7. Prove algebraically that the sum of any odd integer and any even integer is always odd.

(2 marks)

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8. Prove algebraically that the sum of any two consecutive even integers is two more than a multiple of four.

(2 marks)

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9. Prove algebraically that the product of any two consecutive even integers is always a multiple of four.

(2 marks)

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## JP Maths Revision

10. Prove that the product of any two consecutive odd integers is three more than a multiple of four.

(2 marks)

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11. Prove that the sum of any two even integers is always even.

(2 marks)

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# JP Maths Revision

12. Prove that the sum of any two consecutive numbers is odd.

(2 marks)

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13. Prove that the sum of the squares of any two consecutive odd numbers is two more than a multiple of eight.

(3 marks)

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## JP Maths Revision

14. Prove the sum of the squares of two consecutive multiples of four is always a multiple of 16.

(3 marks)

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15. Prove that the difference of the squares of any two consecutive integers is the same as the sum of those two integers.

(3 marks)

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## JP Maths Revision

16. Prove that the sum of any three consecutive even integers is always a multiple of six.

(2 marks)

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17. Prove that the sum of  $n(n + 3)$  and  $3n + 9$  is always a square number for integer values of  $n$ .

(3 marks)

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## JP Maths Revision

18. Prove that  $4(x + 2)^2 + 2(x - 1)^2$  is always a multiple of six for all integer values of  $x$ .

(3 marks)

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19. Prove that  $(7x + 1)^2 - (3x + 1)^2$  is always a multiple of 8 for all integer values of  $x$ .

(3 marks)

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## JP Maths Revision

20. Prove that  $(5x + 1)^2 - (3x + 1)^2$  is always a multiple of 4 for all integer values of  $x$ .

(3 marks)

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21. Prove that the sum  $\frac{1}{2}n(n + 2)$ ,  $\frac{1}{2}n(n + 10)$  and  $4n + 25$  is always a square number for all integer values of  $n$ .

(3 marks)

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## JP Maths Revision

22. Prove that the sum of the squares of any two consecutive even integers is always a multiple of 4.

(3 marks)

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23. Prove that  $(n + 1)^2 + 3n(n + 2) + 10$  is always even for all integer values of  $n$ .

(3 marks)

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# JP Maths Revision

24. Below are the first five terms of an arithmetic sequence

$$3, 7, 11, 15, 19$$

Prove that the difference of the squares of any two consecutive terms is always a multiple of 8.

(3 marks)



25.  $x$  is an integer. Jasmine says that  $x^2 - (x + 3)(x + 5)$  is always negative. Jasmine is wrong. Explain why.

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(2 marks)





## JP Maths Revision

26. Prove that the sum of  $\frac{1}{2}n(n + 6)$ ,  $\frac{1}{2}(n + 2)(n + 4)$  and  $2(3n + 16)$  is always a square number for all integer values of  $n$ .

(3 marks)

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